

# The Lake Trout Rehabilitation Model:

Program Documentation

by

Carl J. Walters

Lawrence D. Jacobson

and

George R. Spangler

Special Publication No. 86-1



**Great Lakes Fishery Commission**

1451 Green Road  
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September 1986

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# The Lake Trout Rehabilitation Model: Program Documentation

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## FOREWORD

The purpose of this report is to describe and document a computer simulation model known as "The Lake Trout Rehabilitation Model" written by Carl Walters. The Lake Trout Rehabilitation Model has its roots in the work of Walters et al. (1980) and in the Sea Lamprey International Symposium (SLIS) that was sponsored by the Great Lakes Fishery Commission and Convened in 1979. Over time, and with the help of numerous individuals, the Lake Trout Rehabilitation Model evolved into its present form. Unlike the models described by Koonce et al. (1982) and Spangler and Jacobson (1985), the Lake Trout Rehabilitation Model was not written by a large team of experts during an adaptive management workshop.

The Lake Trout Rehabilitation Model simulates most aspects of lake trout population biology, including factors that are thought to contribute to delayed rehabilitation of Great Lakes lake trout stocks: 1) mortality due to predation by sea lamprey, 2) fishing mortality, 3) reproductive incompetence of stocked fish and 4) time lags due to the relatively late age at maturity in lake trout. The model is realistic in that it includes the essential features of an age structured population and important biological characteristics of lake trout. It is important to remember, however, that the model does not include some aspects of lake trout biology that may be crucial to the problem of lake trout rehabilitation, notably changes in growth of lake trout due to forage base limitations. Furthermore, the true functional relationships between some of the entities in the model (e.g. mortality of lake trout and abundance of sea lamprey, abundance of sea lamprey and dollars spent for sea lamprey control) are unknown and are represented in the model by "best guesses". For these reasons results obtained using the Lake Trout Rehabilitation Model should be interpreted qualitatively rather than quantitatively.

The Lake Trout Rehabilitation Model simulates rehabilitation of a trout stock from an initial condition of no fish. Rehabilitation is achieved through control of sea lamprey, lake trout stocking and limitations on fishing effort. The rate of rehabilitation depends on how much money is spent on lamprey control, the number of yearling lake trout stocked and the amount of fishing effort; these policy variables are controlled by the person using the model. The model runs quickly (2 1/4 minutes to simulate 30 years) and plots the status of the simulated trout Stock and fishery on the screen at the end of every simulated year. The user can interrupt the simulation at any time in order to change the policy variables. These features are important because they allow the user to experiment with a variety of different policies for lake trout rehabilitation and to continuously monitor the effects of those policies as the simulation progresses. The potential for interactive use of the program and the degree of realism that was obtained make use of the Lake Trout Rehabilitation Model an interesting exercise.

The Lake Trout Rehabilitation Model is written in Applesoft™ BASIC and will run under Disk Operating System 3.3 (DOS 3.3) on any Apple II™ series microcomputer with at least 64K of memory. The model can be obtained on a 5 1/4 inch floppy disk from the Great Lakes Fishery Commission or from George

Spangler. There are two versions of the program: "INTERACTIVE TROUT. ORIGINAL" and "INTERACTIVE TROUT". INTERACTIVE TROUT. ORIGINAL is the original version written by Walters. INTERACTIVE TROUT is a version that was modified by the junior authors. The modifications were made to correct a minor bug and to enhance the readability of the computer code (see Appendix E). The original and modified VerSiOns are both useable and will give similar, though not identical, results.

Functional relationships used in the Lake Trout Rehabilitation Model are described in the main body of this document. Policy analysis (using the modified version) is illustrated in Appendix A. Appendix B gives instructions for running the models. A flow chart and listing of the computer code are given for INTERACTIVE TROUT in Appendices C and D, respectively. Appendix E describes the differences between INTERACTIVE TROUT and INTERACTIVE TROUT.ORIGINAL.

# The Lake Trout Rehabilitation Model:

## Program Documentation

### OVERVIEW

The objective of the Lake Trout Rehabilitation Model is to simulate changes in lake trout abundance using an age structured population model that realistically accounts for: 1) known time lags (between birth, stocking, maturity and recruitment to the fishery), 2) stocking policy, 3) differences in the reproductive capability of wild and stocked fish, 4) natural limits to recruitment (the stock-recruitment relationship and juvenile habitat capacity) and 5) mortality due to natural factors, lamprey predation and fishing. Not included in the model are a number of more controversial relationships such as changes in the forage base, changes in the abundance of alternate hosts for sea lamprey and changes in lake trout habitat due to pollution. The “slow dynamic” of spawning habitat recolonization and adaptation of local stocks is not considered; instead, it is assumed that all major spawning shoals are simultaneously recolonized as abundance of lake trout increases. The model starts from an initial condition of no fish. Abundance of lake trout increases as fish are stocked and as stocked fish begin to reproduce naturally. Thirty years of lake trout rehabilitation are simulated.

### FUNCTIONAL RELATIONSHIPS

The following are detailed descriptions of the important functional relationships in the Lake Trout Rehabilitation Model. Values for constants and initial values of variables are given in parentheses after the quantity is defined.

#### Age Structure

The number of fish age  $a$  in year  $t$  is related to the number of fish age  $a+1$  in year  $t+1$  by:

$$N_{a+1,t+1} = N_{a,t} \exp(-M - v_a q E_t - \lambda_t L_t p / V_t). \quad [1]$$

Where:  $N_{a,t}$  = number of trout age  $a$  in year  $t$ ,  
 $M$  = natural mortality rate in the absence of sea lamprey (constant = 0.3),  
 $v_a$  = relative vulnerability to fishing for trout at age  $a$  (constant, see Table 1 ),

- $q$  = catchability coefficient for fully recruited fish ( $6.0 \times 10^{-7}$ ),
- $E_t$  = fishing effort in year  $t$  (see below),
- $\lambda_t$  = number of trout attacked per lamprey in year  $t$  (see below),
- $L_t$  = lamprey abundance in year  $t$  (see below),
- $\rho$  = probability of a lake trout surviving one lamprey attack (0.4),
- $V_t$  = total number of trout vulnerable to lamprey attack at the start of year  $t$  (all trout age 4-15).

Note that the instantaneous rates for fishing and lamprey induced mortality in [1] are  $v_a q E_t$  and  $\lambda_t L_t \rho / V_t$ , respectively. The maximum age for lake trout is 15 years.

Table 1. Relative vulnerability to fishing by age for lake trout.

Age ( $a$ )	$v_a$
1	0.0
2	0.0
3	0.0
4	0.1
5	0.3
6	0.7
7-15	1.0

### Lamprey mortality

The number of attacks per lamprey in year  $t$  is given by:

$$\lambda_t = \alpha V_t / (\beta + V_t). \quad [2]$$

- Where:
- $\lambda_t$  = the number of attacks per lamprey in year  $t$ ,
  - $\alpha$  = the maximum number of attacks per lamprey (10),
  - $\beta$  = density of lake trout at which  $\lambda_t$  is half the maximum (3000),
  - $V_t$  = abundance of lake trout that are vulnerable to lamprey (all trout age 4-15 in year  $t$ ).

### Natural reproduction

Stocked and wild fish are assumed to mate randomly. Total effective egg deposition is given by:

$$E_t = \sum_{a=m}^{j} N_{a,t} f_a \{R_{t-a} [S_t \bar{\omega}_{WW} + (1 - S_t) \bar{\omega}_{WS}] + (1 - R_{t-a}) [S_t \bar{\omega}_{WS} + (1 - S_t) \bar{\omega}_{WW}]\}. \quad [3]$$

- Where:  $E_t$  = effective egg deposition in year  $t$ ,  
 $R_t$  = the ratio of wild yearlings to total yearlings in year  $t$ ,  
 $S_t$  = the ratio of wild fish to stocked fish in year  $t$ ,  
 $f_a$  = the average fecundity for fish age  $a$ ,  
= proportion mature x proportion female X eggs per female (Table 2),  
 $\bar{\omega}_{WW}$  = relative reproductive success for mating between two wild fish (1.0),  
 $\bar{\omega}_{WS}$  = relative reproductive success for mating between a wild and a stocked fish (0.75),  
 $\bar{\omega}_{SS}$  = relative reproductive success for mating between two stocked fish (0.5),  
 $m$  = the age of maturity (7),  
 $j$  = the maximum age for lake trout (15).

All fish that result from spawning in the lake are assumed to be wild type at spawning time.

Table 2. Average fecundity by age for lake trout.

Age (a)	$f_a$
1-6	0
7	100
8	1000
9	2000
10	3000
11	4,000
12	5,000
13	6,000
14	7,000
15	8,000

### Limits to recruitment

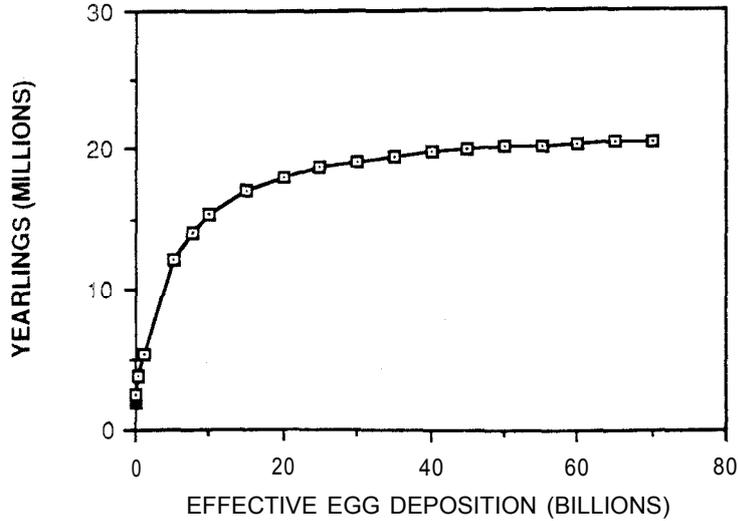
The number of yearling recruits in year  $t+1$  is given by:

$$N_{1,t+1} = S_{t+1} + s_0 E_t / (1 + s_0 E_t / K). \quad [4]$$

- Where:  $N_{1,t+1}$  = total number of yearlings in year  $t+1$ ,  
 $S_{t+1}$  = number of yearlings stocked in year  $t+1$  (2 million),  
 $E_t$  = effective egg deposition in year  $t$ ,  
 $K$  = maximum number (carrying capacity) of wild yearlings (20 million),  
 $s_0$  = maximum survival rate from egg to yearling under uncrowded conditions (0.004).

The relationship between egg deposition and yearlings is illustrated in Figure 1.

Figure 1. Number of yearlings produced as a function of effective egg deposition (assuming 2 million stocked yearlings).



#### Fishing Effort

Fishing effort is a constant fraction of the vulnerable stock until a maximum value is reached:

$$\begin{aligned} E_t &= 0.2 V_t && \{ \text{if } 0.2 N_v \leq E_{max} \} \\ E_t &= E_{max} && \{ \text{if } 0.2 N_v > E_{max} \}, \end{aligned} \quad [5]$$

where  $E_t$  is the fishing effort in year  $t$ ,  $V_t$  is the number of fish vulnerable to fishing in year  $t$  ( $V_t = \sum v_i N_{i,t}$ ) and  $E_{max}$  is the maximum effort (1 million boat days).

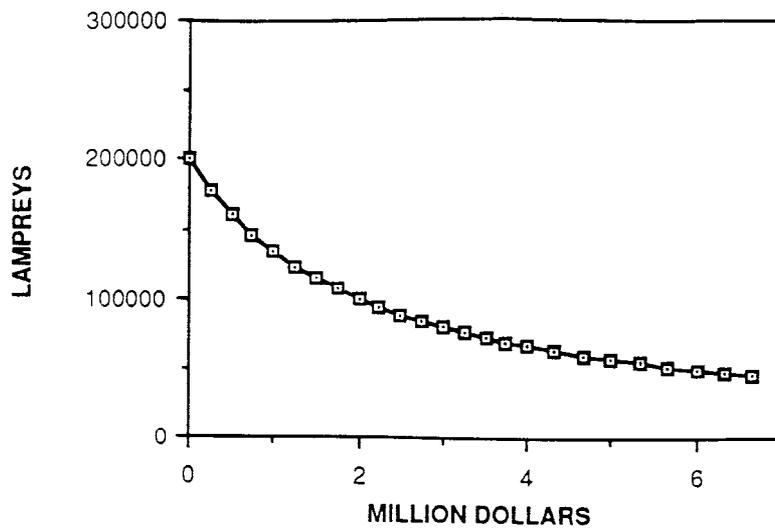
#### Lamprey control by expenditure of money

The relationship between lamprey abundance and dollars spent on lamprey control (Figure 2) is given by:

$$L_t = 200000 / (1 + D_t / 2000000). \quad [6]$$

Where  $L_t$  is the number of lamprey in year  $t$  and  $D_t$  is dollars spent on lamprey control in year  $t$  (6 million dollars). Expenditure of six million dollars gives 50,000 lamprey, expenditure of zero dollars gives 200,000 lampreys.

Figure 2. Number of lamprey as a function of dollars spent on lamprey control.



## REFERENCES

- Eshenroder, R. L., J. F. Kitchell, C. H. Olver, T. P. Poe, and G. R. Spangler. 1984. Overview, p. 44-50. In: R. L. Eshenroder, T. P. Poe, and C. H. Olver [ed.] Strategies for rehabilitation of lake trout in the Great Lakes: proceedings of a conference on lake trout research, August 1983. Great Lakes Fish. Comm. Tech. Rep. No. 40. 63 p.
- Koonce, J. F. [ed.] 1982. A review of the adaptive management workshop addressing salmonid/lamprey management in the Great Lakes. Great Lakes Fish. Comm. Spec. Publ. 82-2. 57 p.
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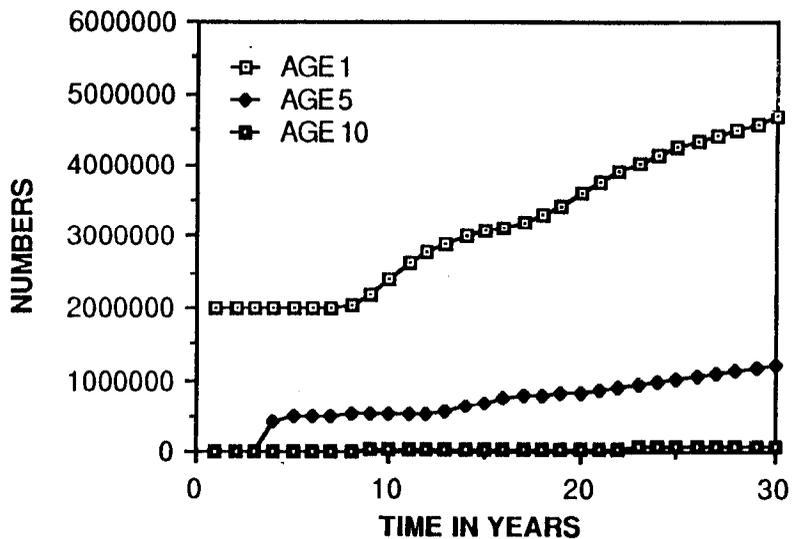
## APPENDIX A

### POLICY Analysis

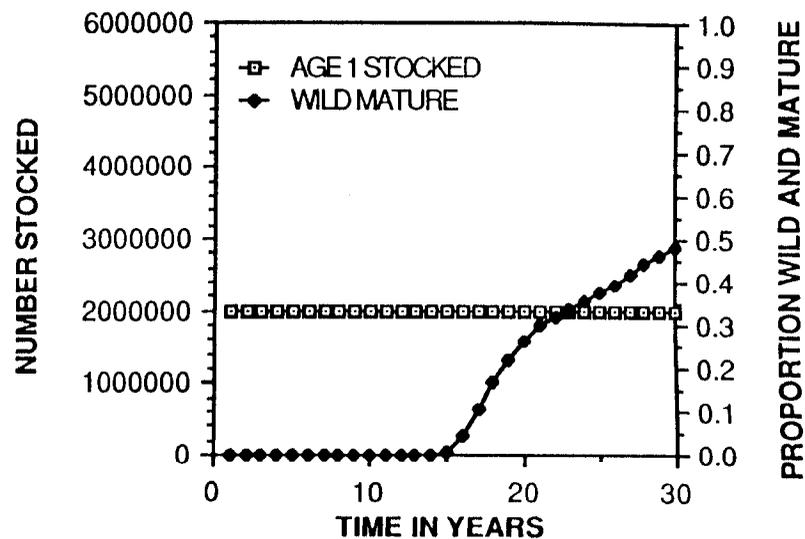
The following examples illustrate the way in which the Lake Trout Rehabilitation Model can be used to investigate the effects Of stocking, harvest and sea lamprey control on rehabilitation of lake trout stocks. There are four examples. The first is a “baseline” scenario in which the number of fish stocked, maximum fishing effort and dollars spent on lamprey control are kept at their initial values (2 million fish, 6 million dollars and 1 million boat days, respectively) through the entire simulation. In the second scenario the amount of money spent for lamprey control is reduced to 2 million dollars (one-third the value used in the baseline case) in order to examine the effects of reduced sea lamprey control on lake trout rehabilitation. Rehabilitation of lake trout in a refuge is depicted in the third example; fishing effort was zero boat days per year through the entire simulation. In the fourth scenario the number of fish stocked is temporarily reduced in year 15 to zero. The effects of a one year interruption in the stocking program are illustrated. Most of these examples are taken from the recommendations by Eshenroder et al. (1985) for large scale field experiments. The axes in the following figures keep the same scale from one scenario to the next in order to facilitate comparison of results from different simulations.

Figure A1. Simulation results for baseline scenario (2 million fish stocked annually, 6 million dollars spent annually for lamprey control, and 1 million boat days per year as the maximum fishing effort). After 30 years of rehabilitation the number of 10 year old fish is negligible, wild fish constitute 50% of the mature stock and the annual catch is 400,000 fish.

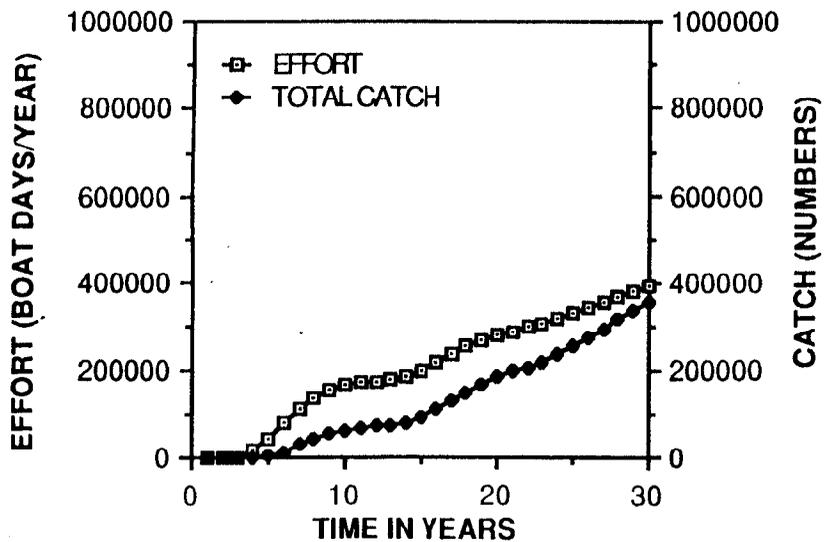
### ABUNDANCE AGES 1, 5, 10



### STOCKING, MATURE SPAWNERS



### FISHING EFFORT, HARVEST



### LAMPREY ABUNDANCE, WOUNDS / FISH

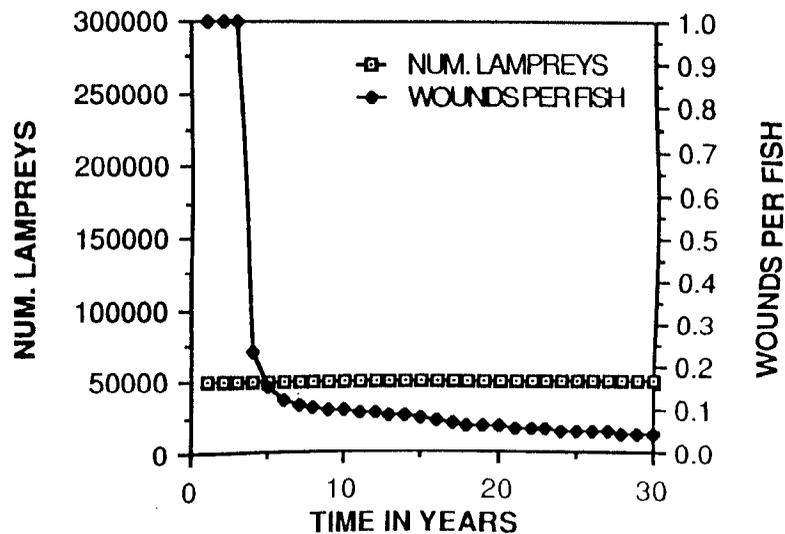
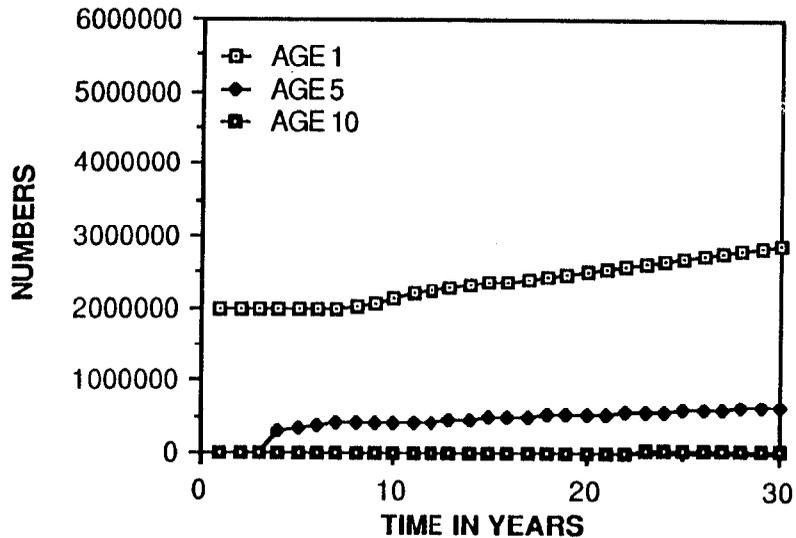
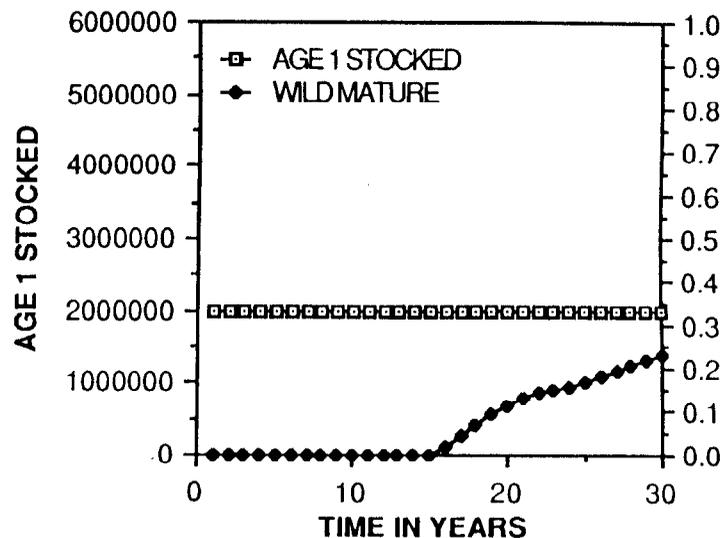


Figure A2. Simulation results for scenario with reduced budget for lamprey control (2 million dollars annually for sea lamprey control, other control variables as in baseline scenario). Note that the rate of rehabilitation is much reduced and that total catch in year 30 is about 1/4 the value obtained in the baseline scenario.

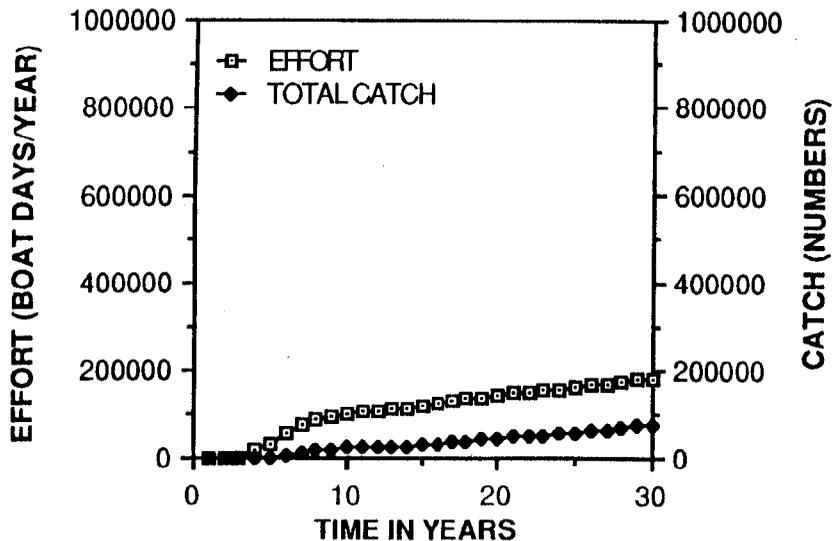
### ABUNDANCE AGES 1, 5, 10



### STOCKING, MATURE SPAWNERS



### FISHING EFFORT, HARVEST



### LAMPREY ABUNDANCE, WOUNDS / FISH

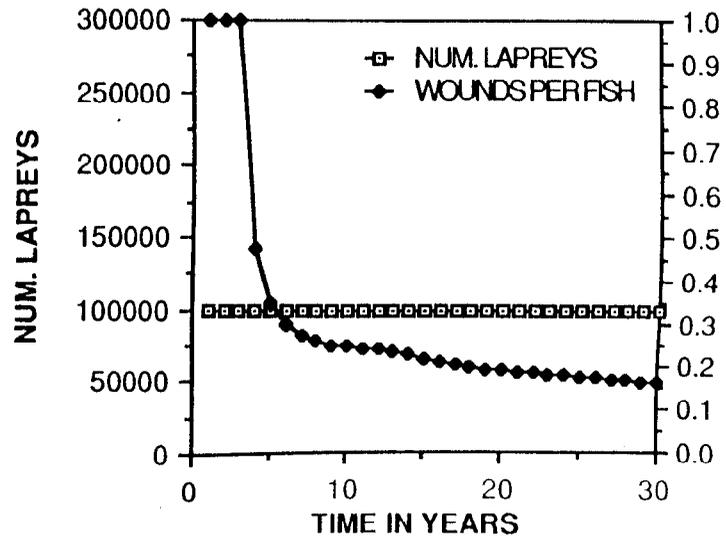
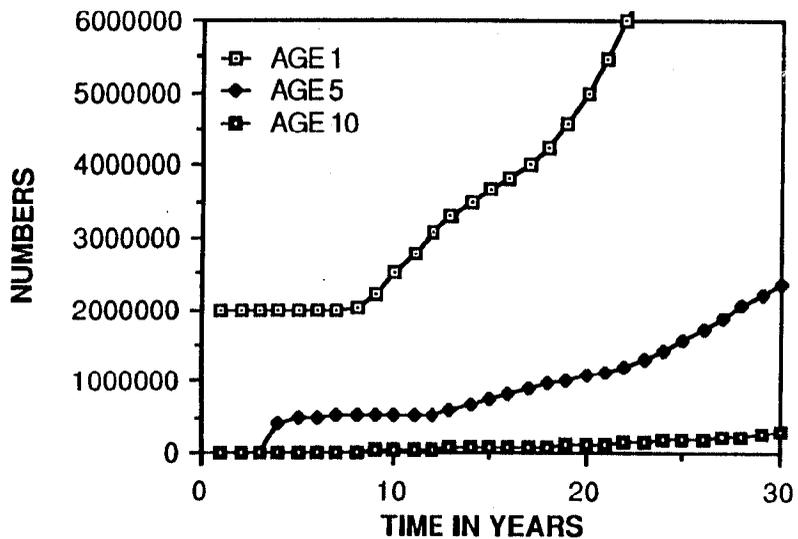
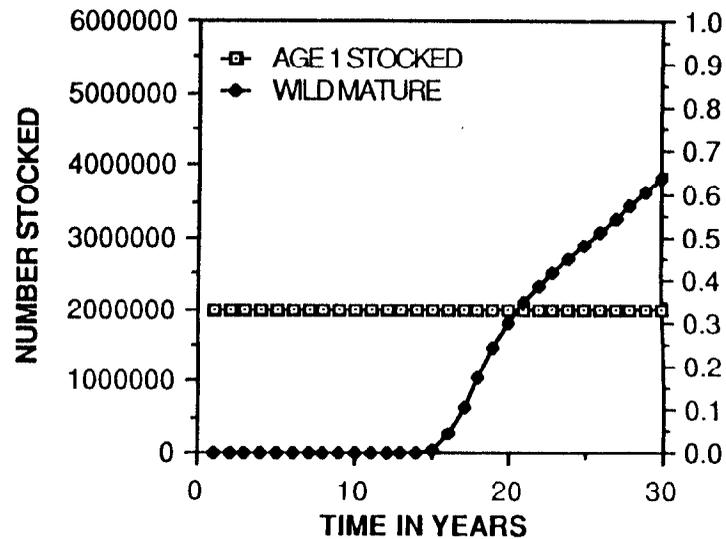


Figure A3. Simulation results for scenario with no fishing effort. This is the only scenario that (gives an appreciable number of 10 year old fish and more than 50% wild fish in the mature stock by year 30.

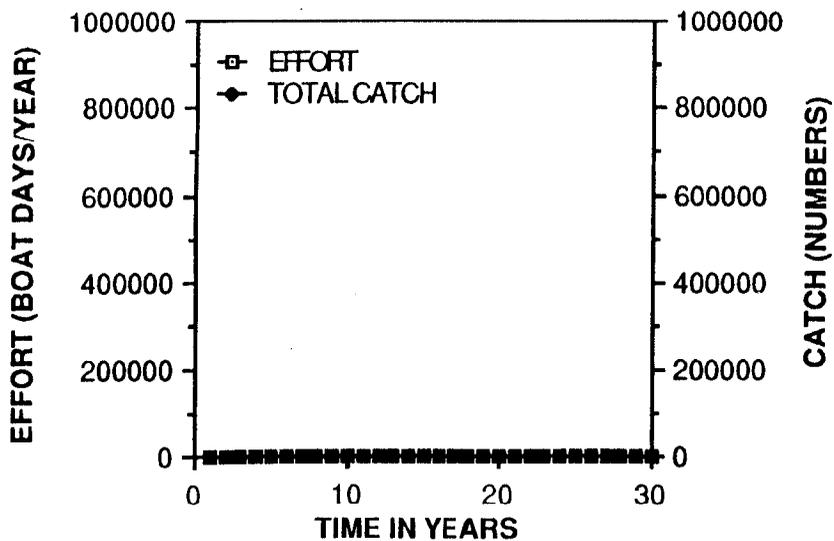
### ABUNDANCE AGES 1, 5, 10



### STOCKING, MATURE SPAWNERS



### FISHING EFFORT, HARVEST



### LAMPREY ABUNDANCE, WOUNDS / FISH

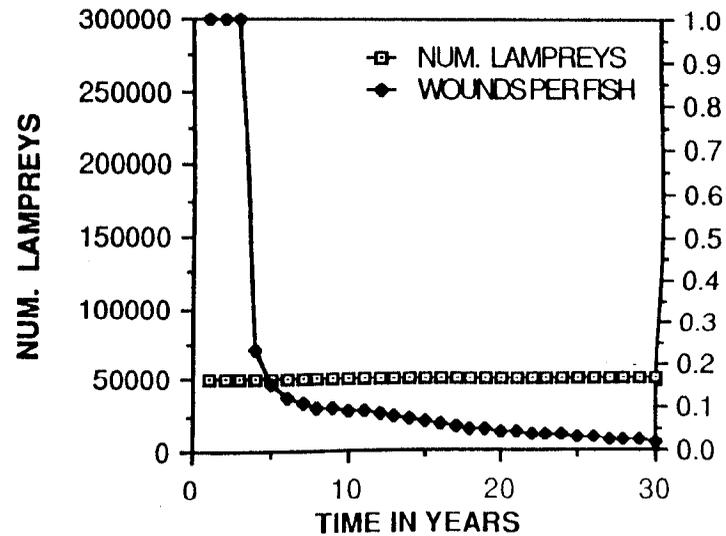
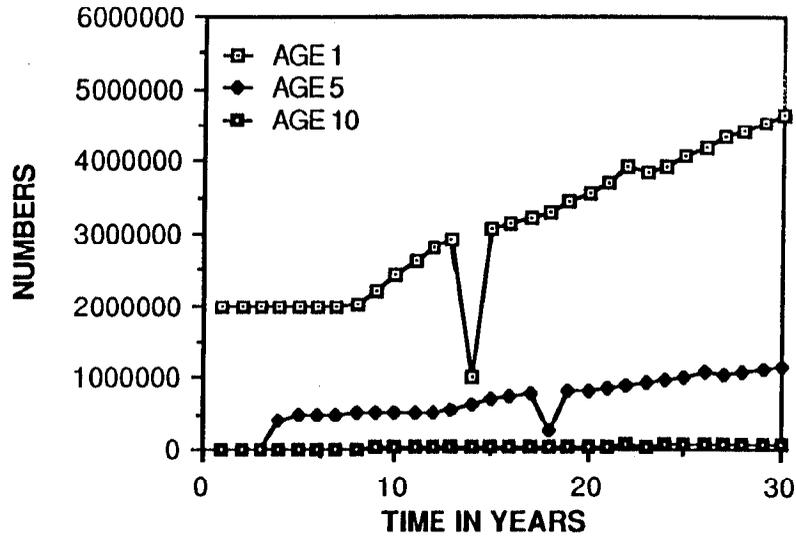
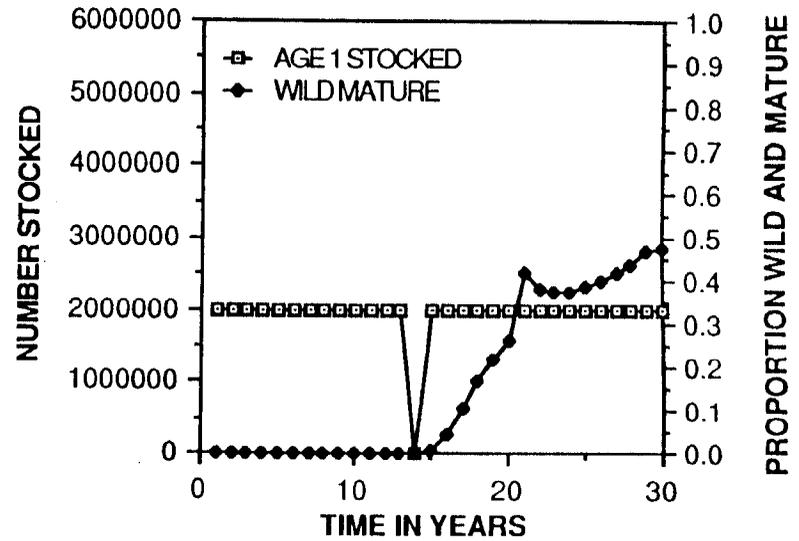


Figure A4. Simulation results for scenario with no fish stocked in year 15 (other policy variables same as for baseline scenario). Note that the number of yearlings in year 16 produced from natural reproduction in year 15 can be clearly seen in the upper right panel. By the end of the simulation, most variables are not much different from the levels obtained in the baseline scenario.

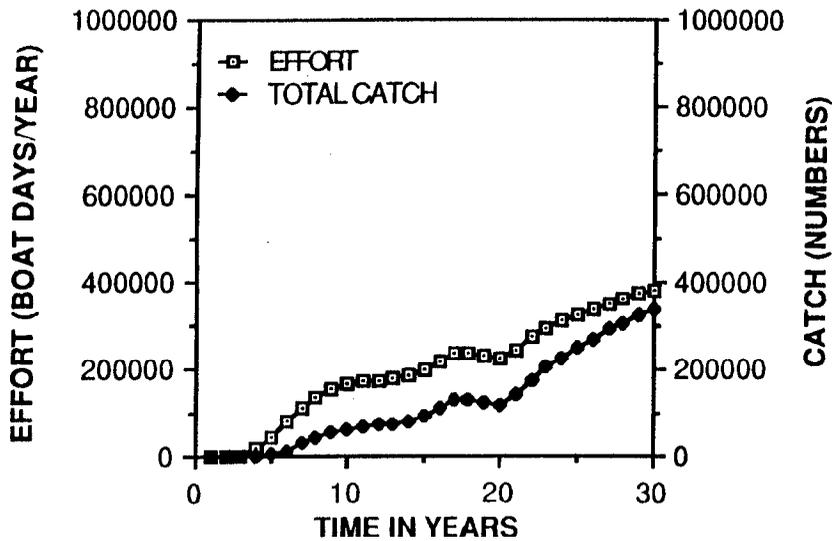
### ABUNDANCE AGES 1, 5, 10



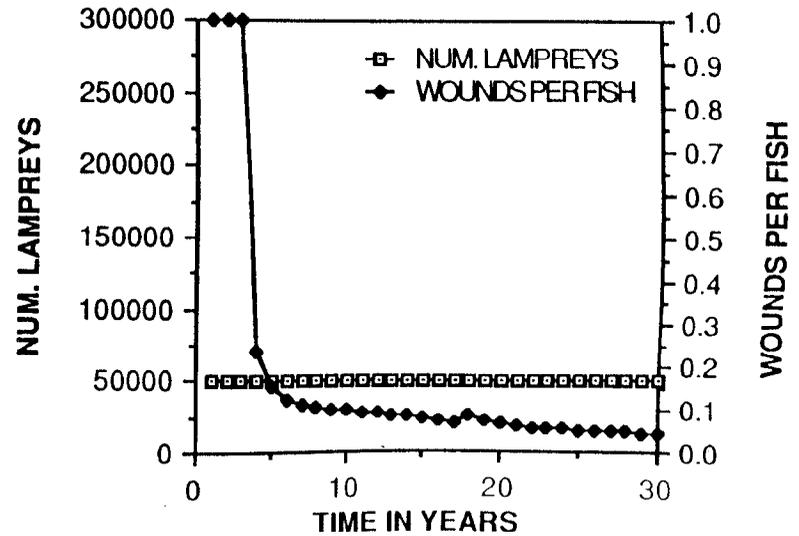
### STOCKING, MATURE SPAWNERS



### FISHING EFFORT, HARVEST



### LAMPREY ABUNDANCE, WOUNDS / FISH



## APPENDIX B

### INSTRUCTIONS FOR RUNNING THE LAKE TROUT REHABILITATION MODEL

Both versions of the Lake Trout Rehabilitation Model (INTERACTIVE TROUT and INTERACTIVE TROUT.ORIGINAL) are written in Applesoft<sup>M</sup> BASIC and run under Disk Operating System 3.3 (DOS 3.3) on an Apple II<sup>TM</sup> series microcomputer with at least 64K of memory. To run either model do the following:

- 1) Insert the disk into the internal disk drive.
- 2) Turn the computer on. When the disk drive stops turning a greeting message is displayed.
- 3) Type "RUN" plus the name of the program plus a carriage return to load a program and run it (e.g. "RUN INTERACTIVE TROUT" followed by a carriage return). You can type "CATALOG" to see the names of the files on the disk.
- 4) The program will ask you to press a key in order to start the simulation.
- 5) If you are using the original version (i.e. INTERACTIVE TROUT.ORIGINAL) then the simulation will commence immediately. If you are using the modified version (i.e. INTERACTIVE TROUT) then the program will give you the opportunity to change the policy variables before the simulation begins. To change a policy variable type the new value plus a carriage return in response to the appropriate prompt. For example, if you type 10000 plus a carriage return in response to the prompt "ANNUAL PLANTING (2000000):" then the number of yearling lake trout planted annually will be changed from the old value (2000000) to the new value (10000). Typing a carriage return only in response to a query will leave a value unchanged. A new value, once entered, is used for the remainder of the simulation or until it is changed again.
- 6) Once the simulation begins, you can interrupt the simulation in order to change the policy variables at any time by pressing the space bar. The program will stop within a few seconds and give you the opportunity to specify new values for the policy variables. Follow the instructions in the instruction above to change a policy variable.
- 7) The numbers of fish in ageclasses 1-9 are printed (in thousands of fish) at the bottom of the screen at the end of every simulated year.

- 8) A number of variables are plotted on the screen at the end of each simulated year. If you have a Color monitor then the plots for different variables will be in different colors. The variables are described in Table B1.
- 9) The model will simulate 30 years of lake trout rehabilitation. At the end of the simulation the program will prompt you to either quit or start a new simulation. Press "Q" to quit or any other key will start a new simulation. If you press "Q" accidentally or change your mind about quitting then type "RUN" or "RUN" plus the version name followed by a carriage return.

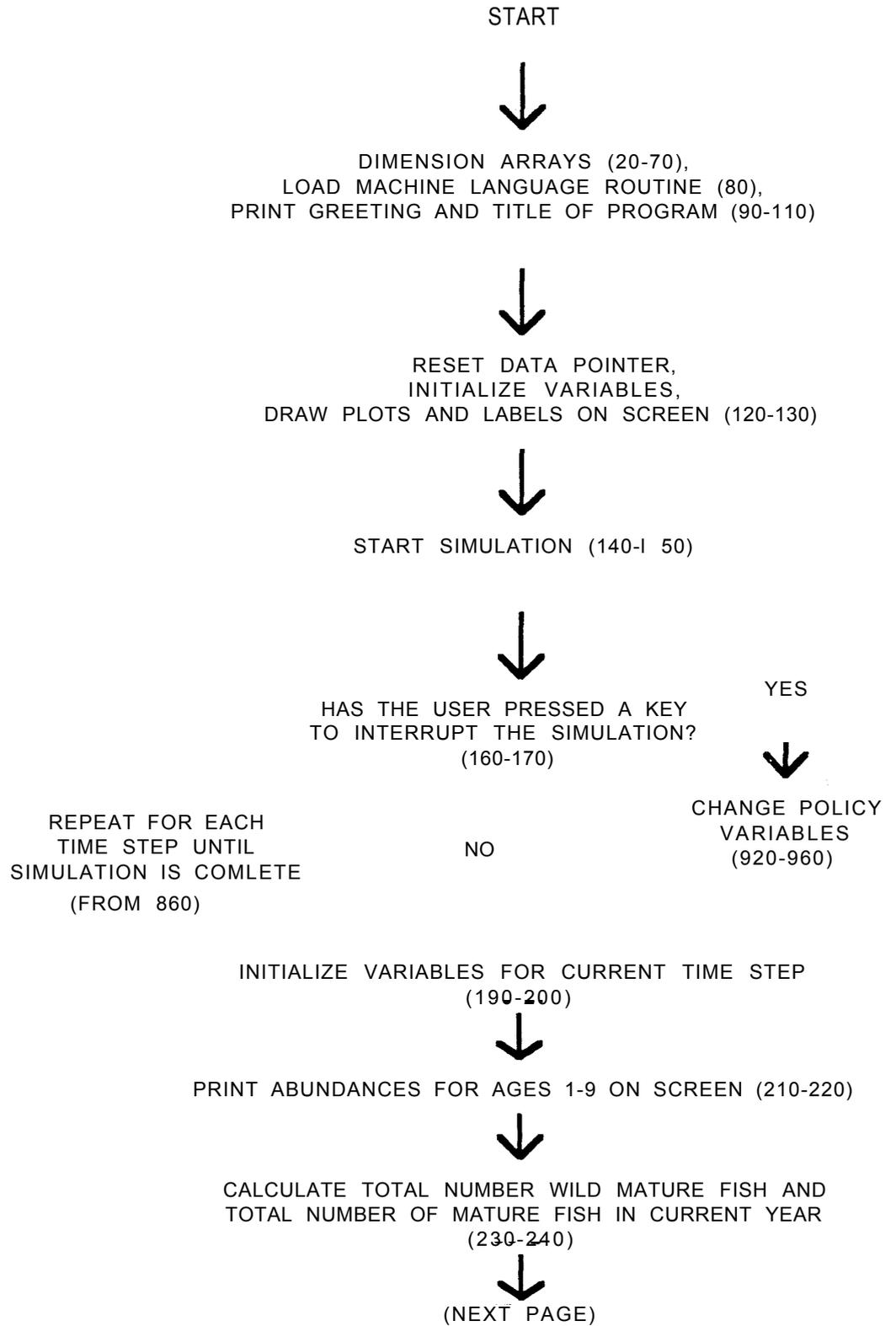
Table B1. Description, plotting color and maximum value for the variables plotted by the Lake Trout Rehabilitation Model.

Description	Color	Maximum Value
Panel 1 (upper left)		
number age 1	white	6 million fish
number age 2	green	6 million fish
number age 3	orange	6 million fish
Panel 2 (upper right)		
% wild yearlings	white	100%
% wild fish age >=5	green	100%
number yearlings stocked	orange	6 million fish
Panel 3 (lower left)		
sport effort	white	10 <sup>6</sup> boat days/year
total catch	green	1 million fish
catch of wild fish	orange	1 million fish
Panel 4 (lower right)		
lamprey wounds per fish	white	1 wound per fish
number sea lamprey	orange	300,000

## APPENDIX C

### FLOWCHART

The following is an informal flowchart that describes the order of computations in the simulation program INTERACTIVE TROUT. Sections of the computer code that draw the graphic images on the screen are omitted from the flowchart for simplicity. The line numbers in the computer program at **which** computations occur are indicated in parentheses.



↓  
CALCULATE PROPORTION WILD MATURE FISH IN CURRENT YEAR  
(250-260)

↓  
CALCULATE TOTAL EFFECTIVE EGG DEPOSITION (270-280)

↓  
CALCULATE NUMBER OF YEARLINGS PRODUCED FROM EGGS LAID  
IN CURRENT YEAR (290-310)

↓  
CALCULATE TOTAL NUMBER OF YEARLINGS (NATURAL REPRODUCTION +  
STOCKING) AND THE PROPORTION WILD YEARLINGS FOR CURRENT YEAR  
(320-330)

↓  
CALCULATE ABUNDANCE OF TROUT VULNERABLE TO LAMPREY (340-350)

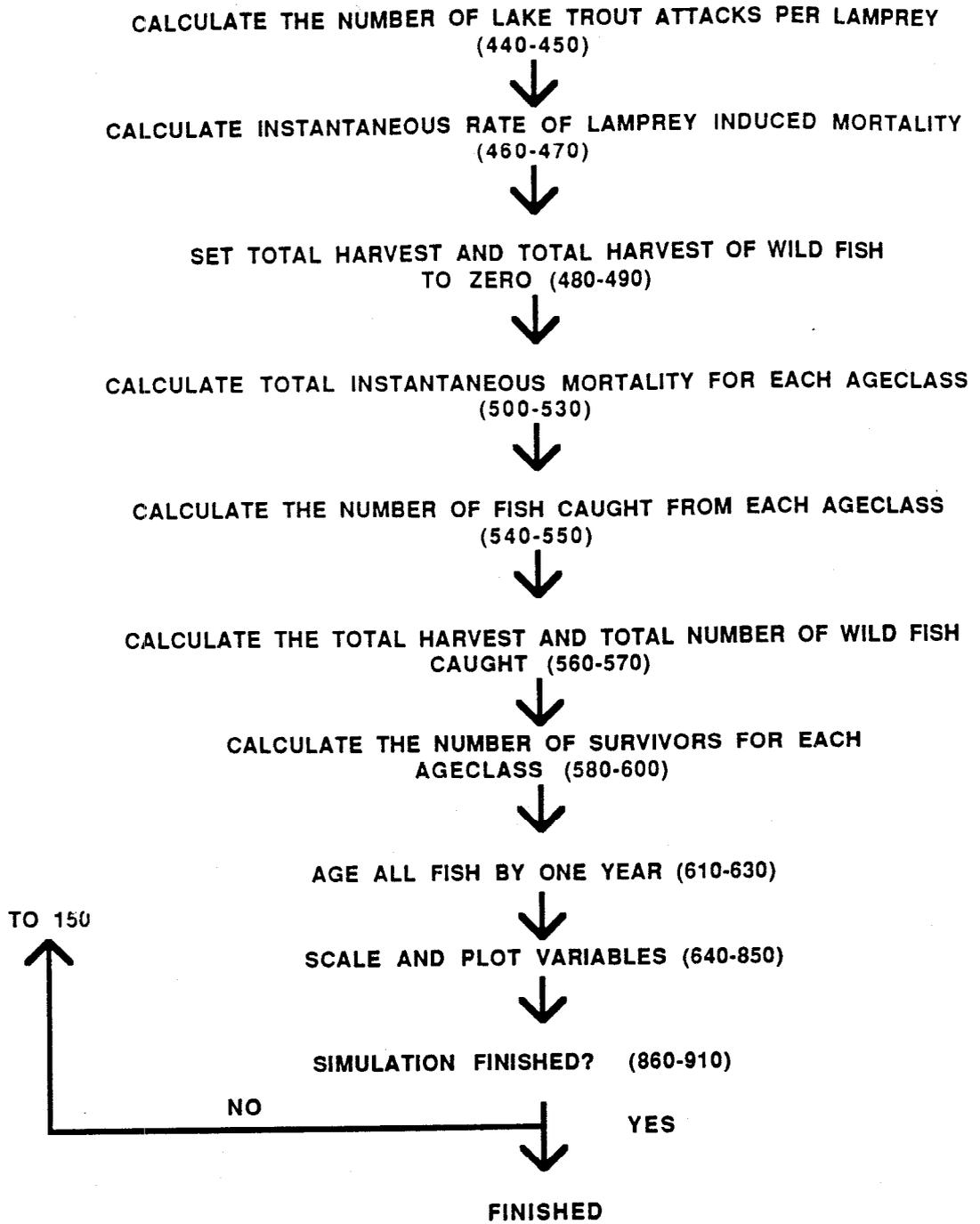
↓  
CALCULATE THE NUMBER OF TROUT VULNERABLE TO FISHING (360-370)

↓  
CALCULATE FISHING EFFORT FOR CURRENT YEAR (380-390)

↓  
CALCULATE INSTANTANEOUS FISHING RATE FOR FULL RECRUITED  
AGECLASSES (400-410)

↓  
CALCULATE THE NUMBER OF LAMPREY FROM DOLLARS SPENT ON  
LAMPREY CONTROL (420-430)

↓  
(NEXT PAGE)



## APPENDIX D

### LISTING of COMPUTER CODE

The following is a complete listing of the Lake Trout Rehabilitation Model named INTERACTIVE TROUT. The dashed lines between lines of computer code are meant to improve readability; they are not part of the code.

VARIABLES, DRAW PLOTTING  
RECTANGLES AND LABELS ON  
SCREEN, THEN GIVE USER A  
CHANGE TO CHANGE  
MANAGEMENT VARIABLES

10 REM PROGRAM INTERACTIVE TROUT BY  
CARL WALTERS, VERSION 8

20 REM Z() ARE VALUES TO BE  
PLOTTED, ZM() ARE MAXIMUM  
VALUES THAT CAN BE  
PLOTTED FOR EACH VARIABLE

30 DIM Z(20), ZM(20)

40 REM N() ARE AGE SPECIFIC  
ABUNDANCES, F() ARE AGE  
SPECIFIC FECUNDITIES, V()  
ARE THE PROPORTION OF  
EACH AGECLASS THAT ARE  
VULNERABLE TO FISHING,  
R() HOLDS THE PROPORTION  
WILD YEARLINGS FOR EVERY  
COHORT IN THE SIMULATION

50 DIM N(20), F(20), V(20), R(50)

60 REM HC() HOLDS THE INTEGER  
VALUES THAT DESIGNATE THE  
COLORS USED TO PLOT THE  
VARIABLES, ZO() HOLDS THE  
ORDINATE VALUE FOR FOR  
THE POINTS PLOTTED IN THE  
LAST TIME STEP

70 DIM ZO(11), ZO(11)

80 PRINT CHR\$(4); "LOAD  
S.T. UPPER/LOWER  
CASE, A\$800"

: POKE 132, 00  
: POKE 233, 08

90 REM PRINT GREETING AND TITLE OF  
PROGRAM

100 TEXT  
: HOME  
: VTAB 10  
: PRINT " LAKE TROUT  
REHABILITATION MODEL"  
: PRINT  
: PRINT "TO CHANGE POLICY IN ANY  
YEAR, SIMPLY HIT SPACE  
BAR"  
: PRINT  
: PRINT "TO BEGIN, HIT ANY KEY"  
: GET A\$  
: PRINT

110 VTAB (24)

120 REM RESET DATA POINTER TO  
FIRST ELEMENT IN DATA  
LIST, INITIALIZE

130 RESTORE  
: GOSUB 1150  
: GOSUB 970  
: GOSUB 920

140 REM START LOOP FOR YEARS 1 TO  
30

150 FOR TI = 0 TO 30

160 REM CHECK AND SEE IF THE  
USER HAS HIT ANY KEYS, IF  
SO THEN ASK USER TO  
MODIFY POLICIES

170 X = PEEK ( - 16384)  
: POKE - 16368, 0  
: IF X > 127 THEN GOSUB 920

180 REM TP = THE CURRENT TIME  
STEP + NUMBER OF  
AGECLASSES, R(TP) HOLDS  
THE PROPORTION WILD  
YEARLINGS IN THE CURRENT  
TIME STEP

190 REM W IS THE NUMBER OF MATURE  
WILD FISH IN THE CURRENT  
YEAR, T IS THE TOTAL  
NUMBER OF MATURE FISH IN  
THE CURRENT YEAR

200 TP = TI + NA  
: W = 0  
: T = 0

210 REM PRINT ABUNDANCES OF  
FIRST 9 AGECLASSES AT  
BOTTOM OF SCREEN (SCALED  
TO UNITS OF 1000 FISH)

220 FOR I = 1 TO 9  
: PRINT INT (N(I) / 1000); " "  
: NEXT  
: PRINT

230 REM CALCULATE TOTAL NUMBER  
OF YEARLINGS IN CURRENT  
YEAR (NATURAL  
REPRODUCTION + STOCKING)  
THEN STORE THE PROPORTION  
WILD YEARLINGS IN CURRENT  
YEAR

240 N1 = W1 + ST  
: R(TP) = W1 / N1

```

250   REM  CALCULATE TOTAL NUMBER OF
      WILD MATURE FISH AND
      TOTAL NUMBER OF MATURE
      FISH FOR CURRENT YEAR
-----
260   FOR A = M TO NA
      :   W = W + R(TP - A) * N(A)
      :   T = T + N(A)
      :   NEXT
-----
270   REM  CALCULATE PROPORTION WILD
      MATURE FISH IN CURRENT
      YEAR
-----
280   PW = W / (T + 1)
      :   IF PW > 1 THEN PW = 0
-----
290   REM  CALCULATE TOTAL EFFECTIVE
      EGG DEPOSITION (E = EGG
      DEPOSITION)
-----
300   RS = (1 - PW) * FS - PW * FC
      :   RW = (1 - PW) * FC - PW * FW
-----
310   E = 0
      :   FOR A = M TO NA
      :   TA = TP - A
      :   E = E + N(A) * F(A) * ((1 -
      :       R(TA)) * RS + R(TA) * RW)
      :   NEXT
-----
320   REM  CALCULATE THE NUMBER OF
      YEARLINGS (W1) PRODUCED
      FROM SPAWNING
-----
330   PM = S1 * E
      :   W1 = PM / (1 + PM / RK) + 0
-----
340   REM  CALCULATE THE ABUNDANCE OF
      TROUT THAT ARE VULNERABLE
      TO LAMPREY (V)
-----
350   V = 0
      :   FOR A = L TO NA
      :   V = V + N(A)
      :   NEXT
-----
360   REM  CALCULATE THE NUMBER OF
      TROUT THAT ARE VULNERABLE
      TO FISHING
-----
370   VS = 0
      :   FOR A = 1 TO NA
      :   VS = VS + V(A) * N(A)
      :   NEXT
-----
380   REM  CALCULATE FISHING EFFORT
      (ES) IN YEAR, IF THE
      FISHING EFFORT IS HIGHER
      THAN THE MAXIMUM ALLOWED
      THEN SET EFFORT EQCAL TO
      THE MAXIMUM
-----
390   ES = AE * VS
      :   IF ES > EM THEN ES = EM
-----
400   REM  CALCULATE THE
      INSTANTANEOUS FISHING
      RATE FOR FULLY RECRUITED
      AGECLASSES
-----
410   FR = QE * ES
-----
420   REM  CALCULATE THE NUMBER OF
      LAMPREY (LT) AS A
      FUNCTION OF THE AMOUNT OF
      MONEY SPENT FOR LAMPREY
      CONTROL
-----
430   LT = L1 / (1 + LX / L2)
-----
440   REM  CALCULATE THE NUMBER OF
      ATTACKS PER LAMPREY
-----
450   LA = AL * V / (BL + V)
-----
460   REM  CALCULATE THE
      INSTANTANEOUS RATE OF
      MORTALITY DUE TO LAMPREY
      (LM)
-----
470   LM = LA * LT * (1 - PL) / V
-----
480   REM  INITIALIZE TOTAL HARVEST
      (H) AND TOTAL HARVEST OF
      WILD FISH (WH)
-----
490   H = 0
      :   WH = 0
-----
500   REM  CALCULATE HARVEST AND
      SURVIVAL FOR EACH
      AGECLASS
-----
510   FOR A = 1 TO NA
-----
520   REM  CALCULATE TOTAL
      INSTANTANEOUS MORTALITY
      AS NATURAL MORTALITY +
      FISHING MORTALITY +
      LAMPREY MORTALITY
-----
530   FA = FR * V(A)
      :   Z = MR + FA
      :   IF A >= L THEN Z = Z + LM
-----
540   REM  CALCULATE THE AGE
      SPECIFIC SURVIVAL RATE
      (SU) AND NUMBER OF FISH
      CAUGHT FROM EACH AGECLASS
      (HA)
-----
550   SU = EXP(-Z)
      :   HA = FA * N(A) * (1 - SU) / Z
-----

```

```

560      REM  CALCULATE THE TOTAL
          HARVEST (H) AND THE TOTAL
          NUMBER OF WILD FISH
          CAUGHT (WH)
-----
570      H = H + HA
          :   WH = WH + HA * R(TP - A)
-----
580      REM  CALCULATE THE NUMBER OF
          SURVIVORS IN EACH
          AGECLASS
-----
590      N(A) = N(A) * SU
-----
600      NEXT
-----
610      REM  AGE ALL THE FISH BY ONE
          YEAR
-----
620      N(NA) = N(NA) + N(NA - 1)
-----
630      FOR A = NA - 1 TO 2 STEP - 1
          :   N(A) = N(A - 1)
          :   NEXT
          :   N(1) = N1
-----
640      REM  CALCULATE POSITION ON X-
          AXES FOR PLOTTING CURRENT
          VALUES (Z1 FOR PLOTS ON
          RIGHT SIDE OF SCREEN AND
          Z2 FOR PLOTS ON LEFT SIDE
          OF SCREEN) AND STORE
          OUTPUT VARIABLES IN Z(I)
          FOR PLOTTING
-----
650      REM  Z(1) IS THE NUMBER OF 1
          YEAR OLDS, Z(2) IS THE
          NUMBER OF 5 YEAR OLDS,
          Z(3) IS THE NUMBER OF 10
          YEAR OLDS, Z(4) IS THE
          NUMBER OF YEARLINGS
          STOCKED, Z(5) IS THE
          PROPORTION WILD MATURE
          FISH
-----
660      Z1 = TI * ZX
          :   Z2 = Z4 + TI * ZX
          :   Z(1) = N(1)
          :   Z(2) = N(5)
          :   Z(3) = N(10)
          :   Z(4) = ST
          :   Z(5) = PW
-----
670      REM  Z(6) IS THE PROPORTION
          WILD YEARLINGS IN CURRENT
          YEAR, Z(7) IS THE SPORT
          EFFORT, Z(8) IS THE
          HARVEST, Z(9) IS THE
          HARVEST OF WILD FISH,
          Z(10) IS THE NUMBER OF
          LAMPREYS, AND Z(11) IS
          LAMPREY WOUNDS PER FISH
-----
-----
680      Z(6) = R(TP)
          :   Z(7) = ES
          :   Z(8) = H
          :   Z(9) = WH
          :   Z(10) = LT
          :   Z(11) = LA * LT * PL / V
-----
690      REM  IF THERE ARE NO FISH
          VULNERABLE TO LAMPREY
          THEN SET WOUNDS PER FISH
          TO 1
-----
700      IF V < 1 THEN Z(11) = 1
-----
710      REM  SCALE THE VALUES BEFORE
          PLOTTING
-----
720      FOR I = 1 TO 6
          :   Z(I) = Z7 * (UN - Z(I)) /
          :           ZM(I))
          :   IF Z(I) < 0 THEN Z(I) = 0
-----
730      NEXT
-----
740      FOR I = 7 TO 11
          :   Z(I) = Z8 + Z7 * (UN - Z(I)) /
          :           ZM(I))
          :   IF Z(I) < Z8 THEN Z(I) = Z8
-----
750      NEXT
-----
760      REM  PLOT THE VALUES
-----
770      IF TI = 0 THEN FOR I = 1 TO 3
          * :   HPLOT Z1,Z(I)
          * :   NEXT
          * :   FOR I = 4 TO 6
          * :   HPLOT Z2,Z(I)
          * :   NEXT
          * :   FOR I = 7 TO 9
          * :   HPLOT Z1,Z(I)
          * :   NEXT
          * :   FOR I = 10 TO 11
          * :   HPLOT Z2,Z(I)
          * :   NEXT
          * :   GOTO 850
-----
780      FOR I = 1 TO 11
          :   HCOLOR= HC(I)
-----
790      ZL = Z3
          :   ZU = Z1
-----
800      IF I < 4 THEN 840
-----
810      IF I > 3 AND I < 7 THEN ZL =
          :           Z9
          * :   ZU = Z2
-----
820      IF I > 6 AND I < 10 THEN 840
-----
830      IF I > 9 THEN ZL = Z9

```

```

* :      ZU = Z2
-----
840      HNPLOT ZL,ZO(I) TO ZU,Z(I)
:      NEXT
-----
850      FOR I = 1 TO 11
:      ZO(I) = Z(I)
:      NEXT
:      Z3 = Z1
:      Z9 = Z2
-----
860      NEXT II
-----
870      PRINT "DONE: TYPE 'Q' TO QUIT,
:              ANY OTHER KEY"
:      PRINT "TO BEGIN NEW SIMULATION"
:      GET Y5
-----
880      REM IF Y5 <> Q THEN BEGIN AGAIN
-----
890      IF Y5 < > "Q" THEN PRINT
* : PRINT
* : PRINT
* : GOTO 130
-----
900      REM IF Y5 = Q THEN QUIT
-----
910      TEXT
:      HOME
:      END
-----
920      VTAB (24)
:      PRINT "MODIFY POLICIES OR RETURN
:              TO KEEP AS IS"
-----
930      PRINT "ANNUAL PLANTING (";ST;
:      INPUT "):";A$
:      IF A$ <> "" THEN ST = VAL (A$)
-----
940      PRINT "LAMPREY CONTROL S (";LX;
:      INPUT "):";A$
:      IF A$ <> "" THEN LX = VAL (A$)
-----
950      PRINT "MAX FISHING EFFORT (";EM;
:      INPUT "):";A$
:      IF A$ <> "" THEN EM = VAL (A$)
-----
960      RETURN
-----
970      HGR
:      HCOLOR= 3
:      ROT= 0
:      SCALE= 1
-----
980      Z7 = 75
:      Z8 = 84
:      UN = 1
:      ZX = 130 / 30
:      Z4 = 149
-----
990      HNPLOT 0,0 TO 0,Z7 TO 130,Z7 TO
:              130,0 TO 0,0
-----
1000     HNPLOT 149,0 TO 149,75 TO 279,75
:              TO 279,0 TO 149,0
-----
1010     HNPLOT 0,84 TO 0,159 TO 130,159 TO
:              130,84 TO 0,84
-----
1020     HNPLOT 149,84 TO 149,159 TO
:              279,159 TO 279,84 TO
:              149,84
-----
1030     HNPLOT 43,73 TO 43,75
:      HNPLOT 43,157 TO 43,159
:      HNPLOT 86,73 TO 86,75
:      HNPLOT 86,157 TO 86,159
-----
1040     HNPLOT 192,73 TO 192,75
:      HNPLOT 192,157 TO 192,159
:      HNPLOT 235,73 TO 235,75
:      HNPLOT 235,157 TO 235,159
-----
1050     ZNS = "NOS AT AGES 1,5,10"
:      X = 5
:      Y = 7
:      GOSUB 1440
-----
1060     ZNS = "EFFORT, CATCHES"
:      X = 5
:      Y = 90
:      GOSUB 1440
-----
1070     ZNS = "PLANTING,%WILD"
:      X = 155
:      Y = 7
:      GOSUB 1440
-----
1080     ZNS = "LAMPREY,WOUNDS/FISH"
:      X = 155
:      Y = 90
:      GOSUB 1440
-----
1090     ZNS = "YEAR:"
:      X = 0
:      Y = 80
:      GOSUB 1440
:      X = 149
:      GOSUB 1440
-----
1100     ZNS = "10"
:      X = 34
:      Y = 80
:      GOSUB 1440
:      X = 193
:      GOSUB 1440
-----
1110     ZNS = "20"
:      X = 77
:      GOSUB 1440
:      X = 226
:      GOSUB 1440
-----
1120     ZNS = "30"
:      X = 121
:      GOSUB 1440

```

```

: X = 265
: GOSUB 1440
-----
1130 RETURN
-----
1140 END
-----
1150 REM THE FOLLOWING CONTAINS
      INITIAL VALUES FOR
      VARIABLES AND CONSTANTS
-----
1160 REM S1 = MAX SURVIVAL RATE
      FROM EGG TO YEARLING, RK
      = CARRYING CAPACITY FOR
      WILD YEARLINGS, PL =
      PROBABILITY OF SURVIVING
      A LAMPREY ATTACK
-----
1170 REM FS = RELATIVE SUCCESS FOR
      STOCKED BY STOCKED
      MATING, FC = RELATIVE
      SUCCESS FOR STOCKED BY
      WILD MATING, FW =
      RELATIVE SUCCESS OF WILD
      BY WILD MATING, AND W1 =
      NUMBER YEARLINGS IN
      CURRENT YEAR FROM EGGS
      PRODUCED LAST YEAR
-----
1180 S1 = .004
      : RK = 20E6
      : PL = .5
      : FS = .5
      : FC = .5
      : FW = .5
      : W1 = .5
-----
1190 REM AL = MAXIMUM ATTACKS PER
      YEAR FOR ONE LAMPREY, BL
      = TROUT DENSITY NEEDED TO
      ACHIEVE 0.5 * AL, MR =
      NATURAL MORTALITY RATE
      (WITHOUT LAM PREY), O = A
      VERY SMALL NUMBER, M =
      AGE AT MATURITY, L = AGE
      AT VULNERABILITY TO
      LAMPREY
-----
1200 AL = 10
      : BL = 30000
      : MR = .3
      : O = 1E - 6
      : M = 7
      : L = 4
-----
1210 REM INITIALIZE AGE SPECIFIC
      FECUNDITIES
-----
1220 DATA
      0,0,0,0,0,0,100,1000,2000
      ,3000,4000,5000,6000,7000
      ,8000
      : FOR I = 1 TO 15
-----
      : READ F(I)
      : NEXT
-----
1230 REM INITIALIZE NUMBERS AT AGE
-----
1240 FOR I = 1 TO 20
      : N(I) = 0
      : NEXT
-----
1250 REM INITIALIZE AGE SPECIFIC
      VULNERABILITIES TO
      FISHING
-----
1260 DATA 0,0,0,.1,.3,.7,1,1,1,1
      : FOR I = 1 TO 10
      : READ V(I)
      : NEXT
      : FOR I = 11 TO 20
      : V(I) = 1
      : NEXT
-----
1270 REM INITIALIZE NUMBER OF
      LAMPREYS (LT), MONEY
      SPENT ON LAMPREY CONTROL
      (LX), NUMBER OF LAMPREYS
      WITH NO LAMPREY CONTROL
      (L1), AND A CONSTANT USED
      TO CALCULATE THE NUMBER
      OF LAMPREY (L2)
-----
1280 LT = 50000
      : LX = 6E6
      : L1 = 2E5
      : L2 = 2E6
-----
1290 REM INITIALIZE NUMBER OF
      YEARLINGS STOCKED
      ANNUALLY
-----
1300 ST = 2E6
-----
1310 REM INITIALIZE INSTANTANEOUS
      FISHING MORTALITY RATE
      (FR), A CONSTANT USED TO
      CALCULATE FISHING EFFORT
      (AE), CATCHABILITY
      COEFFICIENT FOR FULLY
      RECRUITED FISH (QE)
-----
1320 FR = .15
      : AE = .2
      : QE = 6E - 7
-----
1330 REM INITIALIZE THE MAXIMUM
      FISHING EFFORT ALLOWED
      (EM)
-----
1340 EM = 1E6
-----
1350 REM SPECIFY THE NUMBER OF
      AGECLASSES (NA)
-----
1360 NA = 15

```

```

-----
1370  REM  INITIALIZE THE PROPORTION
      WILD YEARLINGS (R(I))
-----
1380  FOR I = 1 TO NA
      :   R(I) = 1E - 9
      : NEXT
-----
1390  REM  SPECIFY THE MAXIMUM VALUES
      THAT CAN BE PLOTTED FOR
      EACH VARIABLE
-----
1400  DATA  6E6,6E6,6E6,6E6,1,1,
           1E6,1E6,1E6,300000,1
      : FOR I = 1 TO 11
      :   READ ZM(I)
      : NEXT
-----
1410  REM  SPECIFY THE COLOR TO BE
      USED FOR PLOTTING EACH
      VARIABLE
-----
1420  DATA  3,1,5,5,1,3,3,1,5,5,3
      : FOR I = 1 TO 11
      :   READ HC(I)
      : NEXT
-----
1430  RETURN
-----
1440  ROT= 0
      : FOR I1 = 1 TO LEN (ZNS)
      :   * = ASC ( MIDS (ZNS,I1,1)) -
           31
      :   IF * < 1 THEN I1 = 1
-----
1450  DRAW I1 AT X + 6 * I1,Y
      : NEXT
      : RETURN
-----
1460  END

```

## APPENDIX E

### MODIFICATIONS BY THE EDITORS TO THE ORIGINAL MODEL

- 1) A comment was added to every line of code that had biological significance.
- 2) The code was renumbered (the first line in the new version is number 10, each line increments by 10).
- 3) The subscript on the vector  $F$  in line 240 of the original version (line 310 in the modified version) was changed from  $A-M$  to  $A$ . The fecundity table in line 10030 of the original model was altered to complement the subscript change (lines 1210-1220 in the modified version). As a result of these changes the fecundity table and egg deposition calculations are indexed by  $age$ . The modifications do not affect numerical results.
- 4) The order of calculations in the original model was changed so that the number of yearlings in year  $t$  is the sum of yearlings produced from spawning in year  $t-1$  and yearlings stocked in year  $t$ . The relevant line numbers are 250-260 in the original version and 240 and 330 in the modified version.

## GREAT LAKES FISHERY COMMISSION

### SPECIAL PUBLICATIONS

- 79-1 Illustrated field guide for the classification of sea lamprey attack marks on Great Lakes lake trout. 1979. E. L. King and T. A. Edsall. 41 p.
- 82-1 Recommendations for freshwater fisheries research and management from the Stock Concept Symposium (STOCS). 1982. A. H. Berst and G. R. Spangler. 24 p.
- 82-2 A review of the adaptive management workshop addressing salmonid/lamprey management in the Great Lakes. 1982. Edited by J. F. Koonce, L. Greig, B. Henderson, D. Jester, K. Minns, and G. Spangler. 40 p.
- 82-3 Identification of larval fishes of the Great Lakes basin with emphasis on the Lake Michigan drainage. 1982. Edited by N. A. Auer. 744 p.
- 83-1 Quota management of Lake Erie fisheries. 1983. Edited by J. F. Koonce, D. Jester, B. Henderson, R. Hatch, and M. Jones. 39 p.
- 83-2 A guide to integrated fish health management in the Great Lakes basin. 1983. Edited by F. P. Meyer, J. W. Warren, and T. G. Carey. 262 p.
- 84-1 Recommendations for standardizing the reporting of sea lamprey marking data. 1984. R. L. Eshenroder, and J. F. Koonce. 21 p.
- 84-2 Working papers developed at the August 1983 conference on lake trout research. 1984. Edited by R. L. Eshenroder, T. P. Poe, and C. H. Olver.
- 84-3 Analysis of the response to the use of "Adaptive Environmental Assessment Methodology\*" by the Great Lakes Fishery Commission. 1985. C. K. Minns, J. M. Cooley, and J. E. Forney. 21 p.
- 85-1 Lake Erie fish community workshop (report of the April 4-5, 1979 meeting). 1985. Edited by J. R. Paine and R. B. Kenyon. 58 p.
- 85-2 A workshop concerning the application of integrated pest management (IPM) to sea lamprey control in the Great Lakes. 1985. Edited by G. R. Spangler and L. D. Jacobson. 97 p.
- 85-3 Presented papers from the Council of Lake Committees plenary session on Great Lakes predator-prey issues, March 20, 1985. 1985. Edited by R. L. Eshenroder. 134 p.
- 85-4 Great Lakes fish disease control policy and model program. 1985. Edited by J. G. Hnath. 24 p.
- 85-5 Great Lakes Law Enforcement/Fisheries Management Workshop (Report of the 21, 22 September 1983 meeting). 1985. Edited by W. L. Hartman and M. A. Ross. 26 p.
- 85-6 TFM vs. the sea lamprey: a generation later. 1985. 17 p.